## A Single Monetary Policy for Heterogeneous Labour Markets: The Case of the Euro Area

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These are the views of the authors and do not represent the views of the Banco de Portugal, European Central Bank, the Central Bank of Ireland, or of the eurosystem.

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## Motivation

Both the ECB and the FED in their recent strategy reviews paid more attention to employment and inequality.

- The ECB: "...the medium-term orientation provides flexibility to take account of employment in response to economic shocks, giving rise to a temporary trade-off between short-term employment and inflation stabilisation without endangering medium-term price stability." and "... important to [...] account for uncertainty, heterogeneity and ongoing structural changes shaping the outlook for economic activity and employment in the euro area and its member countries."
- The FOMC reviewed its strategy and clarified the maximum employment goal. "Our revised statement reflects our appreciation of a strong labour market, particularly for many in low- and moderate-income communities..." (J. Powell)


## Job finding rates by educational attainment in the EA

EA countries differ (trade direction...), but country-specific labour institutions are typical (computed from OECD data):

| Country | Below upp. secondary | Upper sec., non-tertiary | Tertiary |
| :--- | :---: | :---: | :---: |
| Austria | 0.40 | 0.36 | 0.20 |
| Belgium | 0.10 | 0.18 | 0.33 |
| Finland | 0.14 | 0.44 | 0.35 |
| France | 0.14 | 0.19 | 0.20 |
| Germany | $\mathbf{0 . 2 1}$ | $\mathbf{0 . 2 9}$ | $\mathbf{0 . 3 5}$ |
| Greece | $\mathbf{0 . 1 2}$ | $\mathbf{0 . 1 2}$ | $\mathbf{0 . 1 3}$ |
| Hungary | 0.22 | 0.25 | 0.33 |
| Ireland | 0.10 | 0.16 | 0.19 |
| Italy | 0.15 | 0.14 | 0.24 |
| Latvia | 0.16 | 0.19 | 0.26 |
| The Netherlands | 0.25 | 0.26 | 0.35 |
| Slovak Republic | 0.12 | 0.23 | 0.34 |
| Slovenia | 0.28 | 0.07 | 0.30 |
| Spain | $\mathbf{0 . 2 8}$ | $\mathbf{0 . 2 9}$ | $\mathbf{0 . 3 0}$ |

## What we do

- Consider a typical two-agent New Keynesian model:
- Constrained households consume their labour income (minus taxes, plus eventual transfers)...
- ...so their consumption = their disposable income...
- ...so disposable income is the only (!) determinant of their consumption...
- ...and then the typical assumption is that wages of the unconstrained households ("the rich") behave exactly the same as wages of the constrained households ("the poor").
- We relax this assumption and allow for different unemployment rates, matching probabilities, separation rates...
- We look at monetary policy and inflation-(un)employment trade-off


## Model of the euro area and the global econ. (EAGLE)

## Rest of the world

US

Rest of the euro area

Home

## Heterogeneity in the model

- We have several dimensions of heterogeneity in the model:
- Cross-country heterogeneity within the euro area (arising from different trade orientation, etc.)
- Each country is modelled as a two-agent (TANK) model
- Each type of agents has its own labour market segment with search-and-matching
- Each type of agents has their own wage-setting, with the distinction between wages of new hires and existing workers


## Targeting rules

## Benchmark Taylor rule

$$
r_{t}=\varphi_{r} r_{t-1}+\left(1-\varphi_{r}\right)\left(r^{*}+\pi^{*}+\varphi_{\pi}\left(\pi_{t}-\pi^{*}\right)+\varphi_{u} \hat{u}_{t}\right)+\varepsilon_{t}^{R}
$$

Taylor rule with an asymmetric response to unemployment

$$
r_{t}=\varphi_{r} r_{t-1}+\left(1-\varphi_{r}\right)\left(r^{*}+\pi^{*}+\varphi_{\pi}\left(\pi_{t}-\pi^{*}\right)+I_{u>u^{*}} \varphi_{\cup} \hat{u}_{t}\right)+\varepsilon_{t}^{R}
$$

Average inflation targeting rule (4 y-o-y rates)

$$
r_{t}=\varphi_{r} r_{t-1}+\left(1-\varphi_{r}\right)\left(r^{*}+\pi^{*}+\varphi_{\pi}\left(\bar{\pi}_{t}^{T}-\pi^{*}\right)+\varphi_{u} \hat{u}_{t}\right)+\varepsilon_{t}^{R}
$$

## Calibration

We pay particular attention to the calibration of the labour market:

- Compute job finding probabilities for Ricardian and HtM households (OECD, search duration) to match matching efficiencies
- Use replacement ratios from OECD (for Ricardian and HtM) to get vacancy posting costs
- Use unemployment by educational attainment to match separation rates
- Calibrate disutility weight to normalise hours worked to 1 in the steady state


## Simulations

We simulate two types of shocks:

- Inflationary supply shock
- Increase in markups in tradable and non-tradable sectors
- $\Rightarrow$ Monetary policy cannot stabilise output/employment and simultaneously fight inflation
- Expansionary demand shock
- Preference shock and investment-specific demand shock
- $\Rightarrow$ Monetary policy can stabilise output/employment and fight inflation

We look at the performance of the three monetary policy rules, with emphasis on employment and heterogeneity between and within EA countries.

## Inflationary supply shock - EA-wide











## Inflationary supply shock - EA-wide











## Inflationary supply shock - country-specific











[^0]
## Inflationary supply shock - country-specific labour











[^1]
## Expansionary demand shock - EA-wide











## Expansionary demand shock - EA-wide











## Expansionary demand shock - country-specific











[^2]
## Expansionary demand shock - country-specific labour











[^3]
## Key findings

- Responding to unemployment in the EA has the following implications:
- It results in stronger unemployment decrease after expansionary demand shocks and lower unemployment increase after a contractionary supply shock
- It tends to lower inequality between and within EA countries
- It leads to somewhat faster increase in inflation, but also faster return of inflation after a supply shock
- Responding to inflation alone causes large fluctuations between and within EA countries


## BACKUP SLIDES

## Counterfactual on REA - Consumption












## Counterfactual on REA - Wages














-     - . REA, $\phi_{u}=2\left(\right.$ ASUT $\left.\phi_{u}=3\right)-\quad$, REA, $\phi_{u}=0\left(\right.$ ASUT $\left.\phi_{u}=0\right) \cdots \ldots \ldots$ REA, CTF, $\phi_{u}=2\left(\right.$ ASUT $\left.\phi_{u}=3\right) \cdots \cdots \cdots \cdots$ REA, CTF, $\phi_{u}=0\left(A S U T \phi_{u}=\right.$


## Labour market flows

We have 2 segments $s(s=i$ for Ricardian and $s=j$ for HtM$)$ :

$$
n d e_{s, t}=\left(1-\delta_{x, s}\right) n d e_{s, t-1}+M_{s, t}
$$

where $M_{s, t}$ is the number of new matches defined as:

$$
M_{s, t}=\phi_{s, M}\left(u n_{s, t}\right)^{\mu}\left(v a c_{s, t}\right)^{1-\mu}=p_{s, t}^{W} u n_{s, t}=p_{s, t}^{F} v a c_{s, t}
$$

The probability for a searching worker to find a job is

$$
p_{s, t}^{W}=\frac{M_{t}}{u n_{s, t}}=\phi_{s, M}\left(\frac{v a c_{s, t}}{u n_{s, t}}\right)^{1-\mu}
$$

and the probability of a firm finding a worker is

$$
p_{s, t}^{F}=\frac{M_{s, t}}{v a c_{s, t}}=\phi_{s, M}\left(\frac{v a c_{s, t}}{u n_{s, t}}\right)^{-\mu}
$$

## Wages and hiring

We adopt the staggered wage bargaining from Bodart et al. (2006) and de Walque et al. (2009), by labour market segments and by countries (blocs):

- In every segment, for a worker and for a firm, there are two value functions, one for a newly-renegotiated wage $w_{s, t}^{*}$ and one for the existing (average) wage $w_{s, t}$
- Newly-renegotiated wage is determined by Nash bargaining
- Firms hire workers with some probability at newly-renegotiated wage or at an average wage of the period


## Value functions - firm

Let $A^{F}\left(w_{s, t}^{*}\right)$ denote the value of a job for a firm employing a worker from household type $s \in[i, j]$, where $w_{s, j}^{*}$ is the renegotiated wage. It will be convenient to use this value in marginal utility terms, so we define $\mathcal{A}^{F}\left(w_{s, t}^{*}\right) \equiv u^{\prime}\left(c_{s, t}\right) A^{F}\left(w_{s, t}^{*}\right)$. The value of a job with a renegotiated wage for a labour firm can then be written as

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}^{*}\right)= & u^{\prime}\left(c_{s, t}\right)\left(h_{s, t}^{\alpha}, x_{s, t}-h_{s, t}, w_{s, t}^{*}\left(1+\tau_{t}^{w t}\right)\right) \\
& +\beta\left(1-\delta_{x, s}\right)\left[\left(1-\xi_{w, s}\right) \mathcal{A}_{t+1}^{F}\left(w_{s, t+1}^{*}\right)+\xi_{w, s} \mathcal{A}_{t+1}^{F}\left(w_{s, t}^{*}\right)\right]
\end{aligned}
$$

$\mathcal{A}_{t+1}^{F}\left(w_{s, t}^{*}\right)$ prevents to write the expression recursively. But we can write it out:

$$
\begin{aligned}
\mathcal{A}_{t+1}^{F}\left(w_{s, t}^{*}\right) & =u^{\prime}\left(s_{s, t+1}\right)\left(h_{s, t+1}^{\alpha \alpha} x_{s, t+1}-h_{s, t+1} w_{s, t}^{*} \frac{(1+\bar{\pi}) P_{t}}{P_{t+1}}\left(1+\tau_{t+1}^{w t}\right)\right) \\
& +\beta\left(1-\delta_{x, s}\right)\left[\left(1-\xi_{w, s}\right) \mathcal{A}_{t+2}^{F}\left(w_{s, t+2}^{*}\right)+\xi_{w, s} \mathcal{A}_{t+2}^{F}\left(w_{s, t}^{*}\right)\right]
\end{aligned}
$$

## Value functions - firm

If we then substitute in the expression, and repeat this forever, we get

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}^{*}\right) & \left.=\sum_{j=0}^{\infty}\left[\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\right)\right]^{j} u^{\prime}\left(c_{s, t+j}\right)\left(h_{s, t+j}^{\alpha} x_{s, t+j}-h_{s, t+j} w_{s, t}^{*}\left(1+\tau_{t+j}^{w f}\right)\right) \\
& +\sum_{j=0}^{\infty} \beta\left(1-\delta_{x, s}\right)\left(1-\xi_{w, s}\right)\left[\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\right]^{j} \mathcal{A}_{t+j+1}^{F}\left(w_{s, t+j+1}^{*}\right) \\
& +\lim _{j \rightarrow \infty}\left[\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\right]^{j} \mathcal{A}_{t+j+1}^{F}\left(w_{s, t}^{*}\right)
\end{aligned}
$$

The last row goes to 0 . The first row can be written recursively if we define:

$$
\begin{gathered}
S_{s, t}^{X}=u^{\prime}\left(c_{s, t}\right) h_{s, t}^{\alpha H} x_{s, t}+\beta\left(1-\delta_{x, s}\right) \xi_{w, s} S_{s, t+1}^{x} \\
S_{s, t}^{w f}=u^{\prime}\left(c_{s, t}\right) h_{s, t+j}\left(1+\tau_{t+j}^{w f}\right)+\beta\left(1-\delta_{x, s}\right) \xi_{w, s} \frac{(1+\bar{\pi}) P_{t}}{P_{t+1}} S_{s, t+1}^{w f}
\end{gathered}
$$

## Value functions - firm

Using these definitions we can simplify:

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}^{*}\right) & =S_{s, t}^{X}-S_{s, t}^{w f} w_{s, t}^{*} \\
& +\sum_{j=0}^{\infty} \beta\left(1-\delta_{X, s}\right)\left(1-\xi_{w, s}\right)\left[\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\right]^{j} \mathcal{A}_{t+j+1}^{F}\left(w_{s, t+j+1}^{*}\right)
\end{aligned}
$$

This leaves us the infinite sum, but we can forward this equation one period, multiply it with $\beta\left(1-\delta_{X, s}\right) \xi_{w, s}$, and subtract it from both sides of the above equation, which cancels the infinite sum. After some algebra, we finally get the recursive form:

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}^{*}\right) & =\left(S_{s, t}^{x}-S_{s, t}^{w f} w_{s, t}^{*}\right)-\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\left(S_{s, t+1}^{x}-S_{s, t+1}^{w f} w_{s, t+1}^{*}\right)+ \\
& +\beta\left(1-\delta_{x, s}\right) \mathcal{A}_{t+1}^{F}\left(w_{s, t+1}^{*}\right)
\end{aligned}
$$

## Value functions - firm

We can then similarly define the value of a worker with an average wage for a labour firm:

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}\right) & =u^{\prime}\left(c_{s, t}\right)\left(h_{s, t}^{\alpha H} x_{s, t}-h_{s, t} w_{s, t}\left(1+\tau_{t}^{w f}\right)\right) \\
& +\beta\left(1-\delta_{x, s}\right)\left[\left(1-\xi_{w, s}\right) \mathcal{A}_{t+1}^{F}\left(w_{s, t+1}^{*}\right)+\xi_{w, s} \mathcal{A}_{t+1}^{F}\left(w_{s, t}\right)\right]
\end{aligned}
$$

...and after some algebra

$$
\begin{aligned}
\mathcal{A}_{t}^{F}\left(w_{s, t}\right) & =\left(S_{s, t}^{x}-S_{s, t}^{w f} w_{s, t}\right)-\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\left(S_{s, t+1}^{x}-S_{s, t+1}^{w f} w_{s, t+1}\right) \\
& +\beta\left(1-\delta_{x, s}\right) \mathcal{A}_{t+1}^{F}\left(w_{s, t+1}\right)
\end{aligned}
$$

## Value functions - worker

Let $A^{H}\left(w_{s, t}^{*}\right)$ be the value of a job for a worker from household type $s \in[i, j]$, where $w_{s, j}^{*}$ is the renegotiated wage. We use this value in marginal utility terms, so we define $\mathcal{A}^{H}\left(w_{s, t}^{*}\right) \equiv u^{\prime}\left(c_{s, t}\right) A^{H}\left(w_{s, t}^{*}\right)$. The value of a job with a renegotiated wage for a worker is then

$$
\begin{aligned}
\mathcal{A}_{t}^{H}\left(w_{s, t}^{*}\right) & =u^{\prime}\left(c_{s, t}\right)\left(h_{s, t} w_{s, t}^{*}\left(1-\tau_{t}^{w h}\right)-b_{s, t}\right)-\chi \frac{h_{s, t}^{1+\varphi}}{1+\varphi} \\
& +\beta\left(1-\delta_{x, s}\right)\left[\left(1-\xi_{w, s}\right) \mathcal{A}_{t+1}^{H}\left(w_{s, t+1}^{*}\right)+\xi_{w, s} \mathcal{A}_{t+1}^{H}\left(w_{s, t}^{*}\right)\right] \\
& -\beta p_{s, t}^{w}\left[\left(1-\kappa_{w, s}\right) \mathcal{A}_{t+1}^{H}\left(w_{s, t+1}^{*}\right)+\kappa_{w, s} \mathcal{A}_{t+1}^{H}\left(w_{s, t+1}\right)\right]
\end{aligned}
$$

We again have the same problem, so we define

$$
\begin{gathered}
S_{s, t}^{h}=\chi \frac{h_{s, t}^{1+\varphi}}{1+\varphi}+\beta\left(1-\delta_{x, s}\right) \xi_{w, s} S_{s, t+1}^{h} \\
S_{s, t}^{w h}=u^{\prime}\left(c_{s, t}\right) h_{s, t}\left(1-\tau_{t}^{w h}\right)+\beta\left(1-\delta_{x, s}\right) \frac{(1+\bar{\pi})}{\left(1+\pi_{t+1}\right)} \xi_{w, s} S_{s, t+1}^{w h}
\end{gathered}
$$

## Value functions - worker

And we obtain

$$
\begin{aligned}
\mathcal{A}_{t}^{H}\left(w_{s, t}^{*}\right) & =\left(S_{s, t}^{w h}\left(w_{s, t}^{*}-b_{s, t}\right)\right)-\beta\left(1-\delta_{x, s}\right) \xi_{w, s}\left(S_{s, t+1}^{w h}\left(w_{s, t+1}^{*}-b_{s, t+1}\right)\right) \\
& -S_{s, t}^{h}+\beta\left(1-\delta_{X, s}\right) \xi_{w, s} S_{s, t+1}^{h} \\
& +\beta\left[1-\delta_{x, s}-\left(1-\kappa_{w, s}\right) p_{s, t}^{w}\right] \mathcal{A}_{t+1}^{H}\left(w_{s, t+1}^{*}\right)-\beta \kappa_{w, s} p_{s, t}^{w} \mathcal{A}_{t+1}^{H}\left(w_{s, t+1}\right)
\end{aligned}
$$

We do the same for the value function for the average wage of the worker.

## Free entry

A firm posting a vacancy for household type s must pay a per-period constant cost $\psi_{s}$ for having a vacancy open. $\kappa_{w, s}$ is the probability that a firm cannot renegotiate the wage for a newly hired worker from segment $s$. The free-entry condition is:

$$
\psi_{s}=p_{s, t}^{F} \beta \frac{u^{\prime}\left(c_{s, t+1}\right)}{u^{\prime}\left(c_{s, t}\right)}\left[\left(1-\kappa_{w, s}\right) \mathcal{A}_{t}^{F}\left(w_{s, t+1}^{*}\right)+\kappa_{w, s} \mathcal{A}_{t}^{F}\left(w_{s, t+1}\right)\right]
$$

## Wages and hours

Assuming standard (efficient) Nash bargaining between households and labour firms, every period, wages and hours worked are determined by maximising the following expression, where $0<\eta_{s}<1$ measures the bargaining power of workers of type $s$ :

$$
\max _{w_{s, t}^{*}, h_{s, t}}\left(A_{t}^{H}\left(w_{s, t}^{*}\right)\right)^{\eta_{s}}\left(A_{t}^{F}\left(w_{s, t}^{*}\right)\right)^{1-\eta_{s}}
$$

The result is that wages are split according to the Nash sharing rule:

$$
\eta_{s}\left(1-\tau_{t}^{w h}\right) A_{t}^{F}\left(w_{s, t}^{*}\right)=\left(1-\eta_{s}\right)\left(1+\tau_{t}^{w f}\right) A_{t}^{H}\left(w_{s, t}^{*}\right)
$$

Hours are set as:

$$
\alpha_{H} x_{s, t}\left(h_{s, t}\right)^{\alpha_{H-1}}=\frac{\chi}{u^{\prime}\left(c_{s, t}\right)} \frac{\left(1+\tau_{t}^{w f}\right)}{\left(1-\tau_{t}^{w h}\right)}\left(h_{s, t}\right)^{\varphi} .
$$

## Calibrated using data

|  | Home | REA | US | RW |
| :--- | :---: | :---: | :---: | :---: |
| Matching probability, Ricardian workers, $\left(p_{i}^{W}\right)$ | 0.3021 | 0.2238 | 0.5292 | 0.3442 |
| Matching probability, HtM workers, $\left(p_{j}^{W}\right)$ | 0.2090 | 0.1848 | 0.5385 | 0.2598 |
| Matching probability, firms, $\left(p_{s}^{F}\right)$ | 0.70 | 0.70 | 0.70 | 0.70 |
| Matching efficiency, Ric. w., $\left(\varphi_{i, M}\right)$ | 0.4598 | 0.3957 | 0.6086 | 0.4908 |
| Matching efficiency, HtM w. , $\left(\varphi_{j, M}\right)$ | 0.5496 | 0.5363 | 0.6642 | 0.5741 |
| Vac. posting cost, Ric. w., $\left(\Psi_{i}\right)$ | 0.4091 | 0.6768 | 1.1325 | 0.9170 |
| Vac. posting cost, HtM w., $\left(\Psi_{j}\right)$ | 1.2933 | 1.0133 | 0.8246 | 1.1525 |
| Break-up rate, Ric. w., $\left(\delta_{x, i}\right)$ | 0.0203 | 0.0298 | 0.0592 | 0.0344 |
| Break-up rate, HtM w., $\left(\delta_{, j, j}\right)$ | 0.0443 | 0.0348 | 0.1179 | 0.0359 |
| Disutility of labour, Ric. w., $\left(\chi_{i}\right)$ | 1.1481 | 1.2333 | 1.3882 | 1.4416 |
| Disutility of labour, HtM w., $\left(\chi_{j}\right)$ | 4.6902 | 4.2066 | 4.8728 | 4.4392 |
| Replacement ratio, Ric. w., $\left(r r a t_{i}\right)$ | 0.590 | 0.590 | 0.084 | 0.386 |
| Replacement ratio, HtM w., $\left(r r a t_{j}\right)$ | 0.228 | 0.486 | 0.084 | 0.320 |
| Unemployment rate, (un) | 0.0696 | 0.1038 | 0.0605 | 0.0694 |
| Unemployment rate, HtM w., $\left(u n_{j}\right)$ | 0.1437 | 0.1334 | 0.0918 | 0.0930 |

Note: REA=Rest of the euro area; US=United States; RW=Rest of world
Sources: Eurostat (unempl. r.), OECD (repl. r., unempl. r.), BLS (unempl. r.)

## Calibrated based on the literature

|  | Home | REA | US | RW |
| :--- | :---: | :---: | :---: | :---: |
| Inverse of the Frisch elasticity of labour supply $(\zeta)$ | 5.00 | 5.00 | 5.00 | 5.00 |
| Matching elasticity, Ric. $\mathbf{w}$, , $\left(\mu_{i}\right)$ | 0.50 | 0.50 | 0.50 | 0.50 |
| Matching elasticity, HtM w., $\left(\mu_{j}\right)$ | 0.20 | 0.20 | 0.20 | 0.20 |
| Bargaining power, Ric. w., $(\eta)$ | 0.50 | 0.50 | 0.50 | 0.50 |
| Bargaining power, HtM w., $(\eta)$ | 0.50 | 0.50 | 0.50 | 0.50 |
| Prob. to renegotiate existing wage, Ric. $w .,\left(\xi_{w, i}\right)$ | 0.8879 | 0.8879 | 0.8879 | 0.8879 |
| Prob. to renegotiate existing wage, HtM w., $\left(\xi_{w, j}\right)$ | 0.8879 | 0.8879 | 0.8879 | 0.8879 |
| Prob. to start job at avg. wage, Ric. w., $\left(\kappa_{w, i}\right)$ | 0.7 | 0.7 | 0.7 | 0.7 |
| Prob. to start job at avg. wage, HtM w., $\left(\kappa_{w, j}\right)$ | 0.7 | 0.7 | 0.7 | 0.7 |

Note: REA=Rest of the euro area; US=United States; RW=Rest of world
Sources: De Walque et al. (2009), Petrongolo and Pissarides (2001)

## Contractionary demand shock - EA-wide











## Contractionary demand shock - EA-wide











## Contractionary demand shock - country-specific











[^4]
## Contractionary demand shock - country-specific labour









[^5]
[^0]:    ——REA, $\phi_{\mathrm{e}}=2$ - - . REA, $\phi_{\mathrm{u}}=0 \ldots \ldots .$. REA, ASUT, $\phi_{\mathrm{u}}=3 —$ Home, $\phi_{\mathrm{u}}=2 \quad-\quad$. Home, $\phi_{\mathrm{u}}=0 \ldots \ldots .$. Home, ASUT, $\phi_{\mathrm{u}}=3$

[^1]:    

[^2]:    

[^3]:    

[^4]:    

[^5]:    

